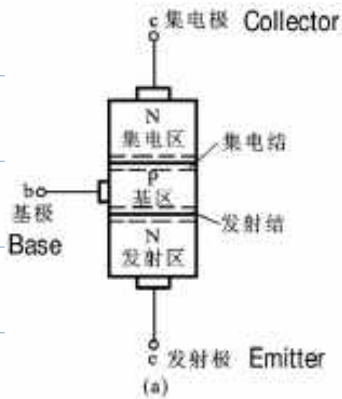


§5 双极结型三极管及其放大电路

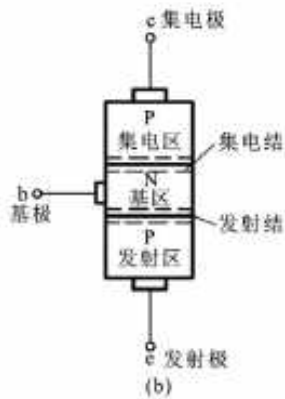
1 双极结型三极管的结构及工作原理

Bipolar Junction Transistor

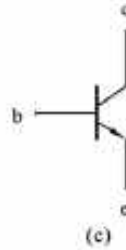
BJT



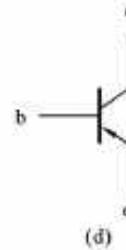
NPN型管结构示意图



PNP型管结构示意图



NPN型管
电路符号



PNP型管
电路符号

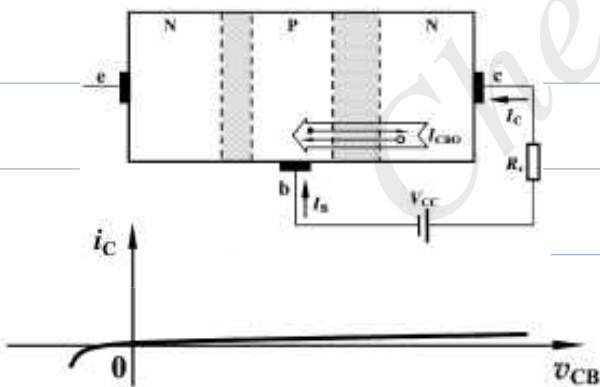
箭头方向:

发射结方向 P→N

结构特点

- ① 发射区的掺杂浓度最高
- ② 集电区掺杂浓度最低，且面积大
- ③ 基区很薄，一般在几微米至几十个微米，且掺杂浓度低于发射区

工作原理

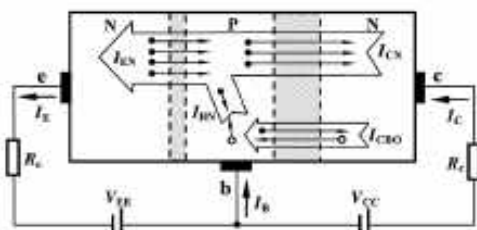


V_{CC} 使集电结反向偏置

促进少子漂移 (少子由本征激发产生)

少子形成漂移电流 I_{CBO}

I_{CBO} 集电结反向饱和电流



V_{EE} 使发射结正向偏置

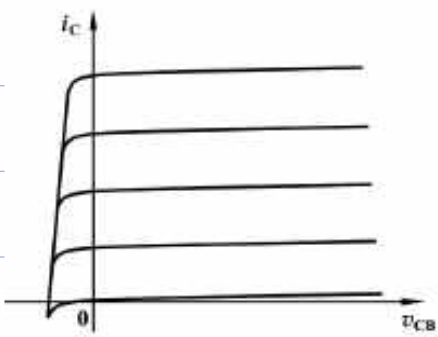
促进多子扩散，产生发射结电流 I_{EN}

(多子是掺杂引起的，不受温度影响)

基区复合电流 I_{BN}

$$I_E = I_{EN} \quad I_B = I_{BN} \quad I_C = I_{CN} + I_{CBO}$$

$$I_E = I_{ES} (e^{\frac{V_{BE}}{V_T}} - 1)$$



发射极电流 I_E 可以控制集电极电流 I_C

控制关系:

$$V_{BE} \rightarrow I_E \rightarrow I_C$$

电流放大系数

$$\alpha = \frac{\text{传输到集电极的电流}}{\text{发射极注入电流}} = \frac{I_{CN}}{I_E} \approx \frac{I_C}{I_E} \quad I_C = \alpha I_E$$

$$\beta = \frac{I_C}{I_B} = \frac{I_C}{I_E - I_C} = \frac{\alpha}{1 - \alpha}$$

反映载流子在基区的复合比例, α/β 越大, 复合比例越低.

BJT 控制关系 \Rightarrow 电流控制器件

$$I_C = \alpha I_E \quad I_C = \beta I_B \quad I_E = (1 + \beta) I_B$$

工作条件 发射结正偏, 集电结反偏

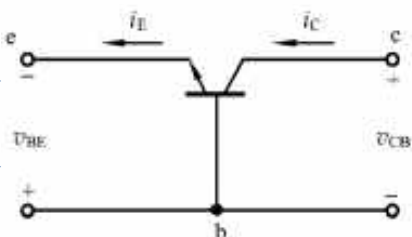
输入: 发射极电流 I_E / 基极电流 I_B

输出: 集电极电流 I_C

组态: 共基极, 共射极, 共集电极

2 BJT 的特性曲线

(1) 共基极

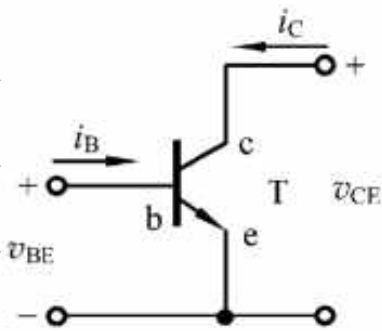


输入特性 $i_E = f(V_{BE}) |_{V_{CB} = \text{const}}$

基本关系 $i_E = I_{ES} (e^{\frac{V_{BE}}{V_T}} - 1)$

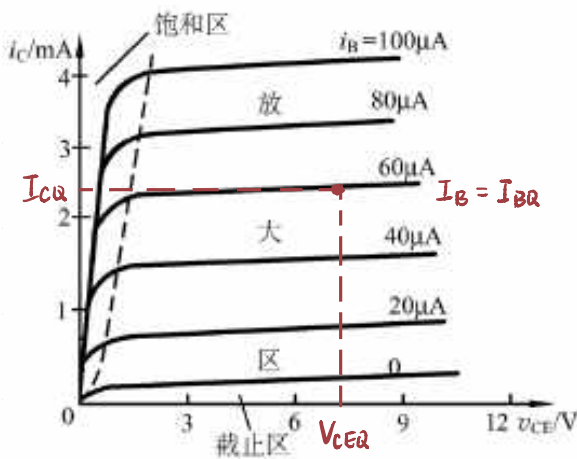
输出特性 $i_C = f(V_{CB}) |_{V_{BE} = \text{const}}$

(2) 共发射极



输入特性 $i_B = f(v_{BE}) \mid v_{CE} = \text{const}$

输出特性 $i_C = f(v_{CE}) \mid v_{BE} = \text{const}$



截止区 $i_C = 0$

饱和区 i_C 随 v_{CE} 增大迅速上升, 通常 $v_{CE} < 0.7V$ (硅)
无法区分不同 i_B 产生的影响

发射结正偏, 集电结正偏或反偏电压很小

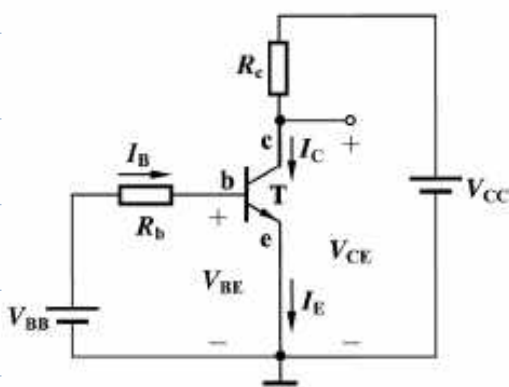
放大区 $i_C = \beta i_B$ i_C 与 v_{CE} 无关 (理想)

发射结正偏, 集电结反偏

静态工作点 Q 点: I_{BQ} , I_{CQ} , V_{CEQ}

3 BJT 的静态偏置和放大电路构成

BJT 的偏置满足: 发射结有合适的正偏, 集电结有合适的反偏.



V_{BB} 提供正向偏置

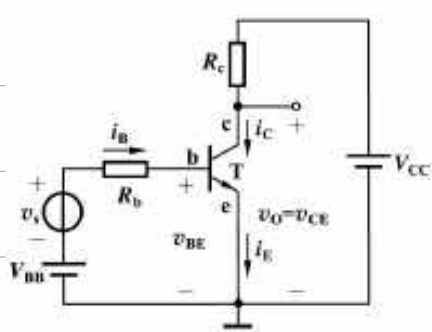
选择合适的 R_B , R_C , 使 $V_C > V_B$, 集电结反偏
求静态工作点.

输入回路 $I_{BQ} = \frac{V_{BB} - V_{BEQ}}{R_B}$

BJT 电流关系 $I_{CQ} = \beta I_{BQ}$

输出回路 $V_{CEQ} = V_{CC} - I_{CQ} R_C$

其中, 一般硅管 $V_{BEQ} = 0.7V$, 锗管 $V_{BEQ} = 0.2V$



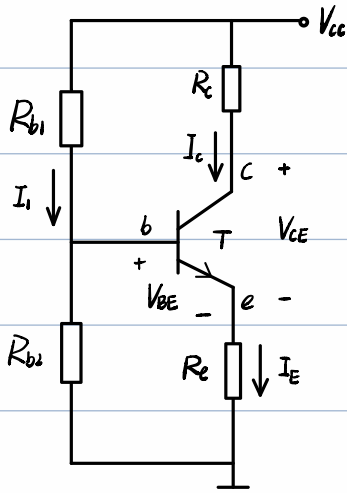
输入信号后 $V_{BE} = V_{BB} + v_s - i_b R_b$

$$i_B = I_{BQ} + i_b$$

$$i_C = \beta i_b$$

$$v_o = v_{CE} = V_{CC} - i_C R_c$$

EXP 基极分压射极偏置电路



当满足 $I_1 \gg I_B$ 时

$$V_{BQ} = \frac{R_{b2}}{R_{b1} + R_{b2}} V_{CC}$$

$$I_{CQ} \approx I_{EQ} = \frac{V_{BQ} - V_{BEQ}}{R_e}$$

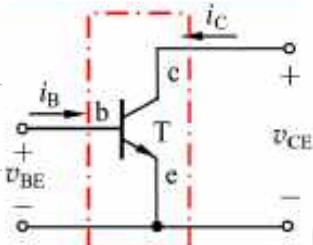
$$V_{CEQ} = V_{CC} - I_{CQ} R_c - I_{EQ} R_e \approx V_{CC} - I_{CQ} (R_c + R_e)$$

$$I_{BQ} = \frac{I_{CQ}}{\beta}$$

检验是否满足 $I_1 \gg I_B$

4 BJT 放大电路的小信号模型分析法

(一) H 参数及小信号模型



输入特性 $i_B = f(v_{BE}) |_{V_{CE} = \text{const}}$

输出特性 $i_C = f(v_{CE}) |_{V_{BE} = \text{const}}$

$$v_{BE} = f_1(i_B, V_{CE}) \quad i_C = f_2(i_B, V_{CE})$$

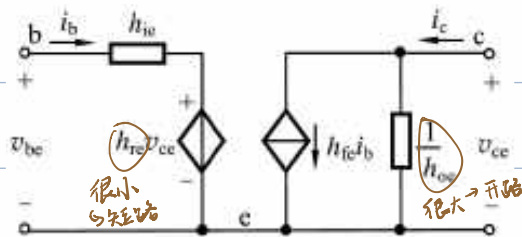
取全微分

$$dv_{BE} = \frac{\partial v_{BE}}{\partial i_B} di_B + \frac{\partial v_{BE}}{\partial V_{CE}} dV_{CE}$$

$$di_C = \frac{\partial i_C}{\partial i_B} di_B + \frac{\partial i_C}{\partial V_{CE}} dV_{CE}$$

$$v_{be} = h_{ie} i_b + h_{re} v_{ce}$$

$$i_c = h_{fe} i_b + h_{oe} v_{ce}$$



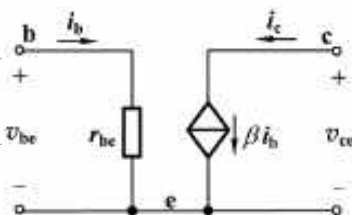
$$h_{ie} = \frac{\partial v_{BE}}{\partial i_B} = r_{be}$$

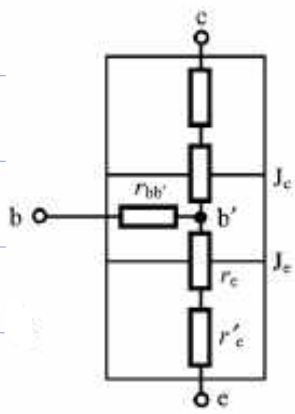
$$h_{re} = \frac{\partial v_{BE}}{\partial V_{CE}} = 10^{-3} \sim 10^{-4}$$

$$h_{fe} = \frac{\partial i_C}{\partial i_B} = \beta$$

$$h_{oe} = \frac{\partial i_C}{\partial V_{CE}} = \frac{1}{r_{ce}}$$

简化





$$r_{be} = \frac{U_{be}}{i_b} = \frac{i_b r_{bb'} + i_e (r_e + r_e')}{i_b} = \frac{i_b r_{bb'} + (1+\beta) i_b (r_e + r_e')}{i_b}$$

$$= r_{bb'} + (1+\beta)(r_e + r_e') \approx r_{bb'} + (1+\beta)r_e$$

常温下发射结电阻 $r_e = \frac{V_T (\text{mV})}{I_{EQ} (\text{mA})} = \frac{26 \text{ mV}}{I_{EQ} (\text{mA})} \approx \frac{26 \text{ mV}}{I_{CE} (\text{mA})}$

低频小功率管 $r_{bb'} \approx 200 \Omega$

$$r_{be} \approx 200 \Omega + (1+\beta) \frac{26 \text{ mV}}{I_{CE} (\text{mA})} \quad r_{ce} = \frac{V_A}{I_{CE}}$$

注意

- ① BJT必须工作在放大区,并且是小信号情况,模型才是可用的。
- ② 只用于交流信号或变化量的分析,不能用来分析静态工作点
- ③ r_{be} 和 r_{ce} 与静态工作点的位置有关, r_{be} 更敏感
- ④ 受控源 βi_b 的电流方向与控制电流 i_b 方向关联

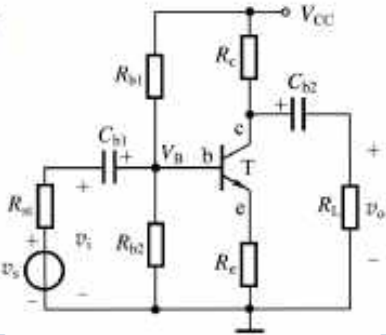
(二) 用小信号模型分析放大电路

EXP 已知 $V_{CC} = 16 \text{ V}$, $R_{b1} = 56 \text{ k}\Omega$, $R_{b2} = 20 \text{ k}\Omega$, $R_c = 3.3 \text{ k}\Omega$,

$R_L = 6.2 \text{ k}\Omega$, $R_{s1} = 500 \Omega$,

BJT的 $\beta = 80$, $r_{ce} = 100 \text{ k}\Omega$, $V_{BEQ} = 0.7 \text{ V}$,

求 A_v , R_i , $A_{vs} = \frac{v_o}{v_s}$, R_o



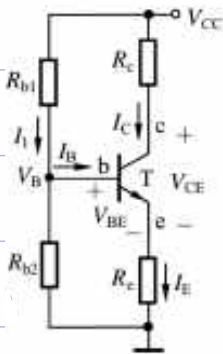
(1) 静态, 设 $I_{BQ} \ll I_1$

$$V_{BQ} = \frac{R_{b2}}{R_{b1} + R_{b2}} V_{CC}$$

$$I_{CQ} \approx I_{EQ} = \frac{V_{BQ}}{R_e} = \frac{V_{BQ} - V_{BEQ}}{R_e}$$

$$V_{CEQ} = V_{CC} - I_{CQ} R_c - I_{EQ} R_e \approx V_{CC} - I_{CQ} (R_c + R_e)$$

$$I_{BQ} = \frac{I_{CQ}}{\beta} \quad \text{求出 } I_{EQ} \approx 1.76 \text{ mA}$$



(2) 动态

H参数 $r_{be} = 200 \Omega + (1+\beta) \frac{26 \text{ mV}}{I_{EQ} (\text{mA})} \approx 1.4 \text{ k}\Omega$

$$v_o = -i_c (R_c \parallel R_L) = -\beta i_b (R_c \parallel R_L)$$

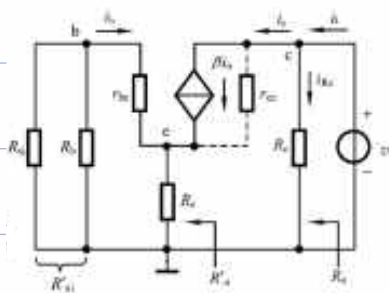
$$v_i = i_b r_{be} + i_e R_e = i_b r_{be} + (1+\beta) i_b R_e$$

$$A_v = \frac{v_o}{v_i} = - \frac{\beta (R_c \parallel R_L)}{r_{be} + (1+\beta) R_e} \approx -1.05$$

$$i_i = i_b + i_{R_b} = \frac{v_i}{r_{be} + (1+\beta) R_e} + \frac{v_i}{R_{b1}} + \frac{v_i}{R_{b2}}$$

$$R_i = \frac{v_i}{i_i} = \frac{1}{\frac{1}{r_{be} + (1+\beta)R_e} + \frac{1}{R_{b1}} + \frac{1}{R_{b2}}} = R_{b1} \parallel R_{b2} \parallel [r_{be} + (1+\beta)R_e] \approx 13.52 \text{ k}\Omega$$

$$A_{v_s} = \frac{v_o}{v_s} = \frac{v_o}{v_i} \cdot \frac{v_i}{v_s} = A_v \cdot \frac{R_i}{R_{s_i} + R_i} \approx -1.01$$



基极回路 KVL: $v_b (r_{be} + R'_{s_i}) + (i_b + i_c) R_e = 0$

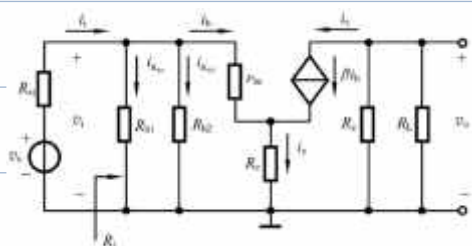
其中 $R'_{s_i} = R_{s_i} \parallel R_b$ $R_b = R_{b1} \parallel R_{b2}$

集电极回路 KVL: $v_c - (i_c - \beta i_b) r_{ce} - (i_b + i_c) R_e = 0$

$R'_o = \frac{v_c}{i_c}$ $R_o = R'_o \parallel R_c$

5 BJT的三种基本放大电路和复合管

(1) 共射极



输入回路 $v_i = i_b r_{be} + (1+\beta) i_b R_e$

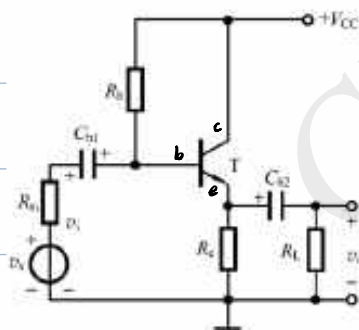
输出回路 $v_o = -\beta i_b (R_c \parallel R_L)$

$$A_v = \frac{v_o}{v_i} = -\frac{\beta (R_c \parallel R_L)}{r_{be} + (1+\beta) R_e}$$

输入电阻 $R_i = R_{b1} \parallel R_{b2} \parallel [r_{be} + (1+\beta) R_e]$

输出电阻 $R_o = R'_o \parallel R_c \approx R_c$

(2) 共集电极



(1) 静态分析

输入回路 $V_{cc} - V_{BEQ} - I_{BQ} R_b - (1+\beta) I_{BQ} R_e = 0$

$$\Rightarrow I_{BQ} = \frac{V_{cc} - V_{BEQ}}{R_b + (1+\beta) R_e}$$

$$I_{CQ} = \beta I_{BQ} \approx I_{EQ}$$

输出回路 $V_{CEQ} = V_{cc} - I_{EQ} R_e$

(2) 动态分析

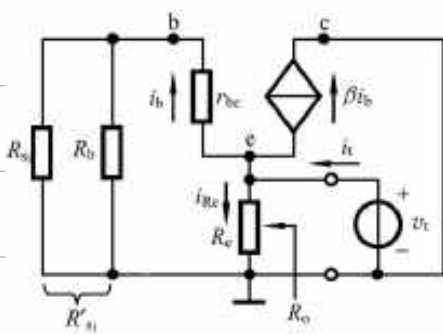
$$r_{be} = 200 \Omega + (1+\beta) \frac{26 \text{ mV}}{I_{CQ} (\text{mA})}$$

$$v_i = i_b r_{be} + (1+\beta) i_b (R_e \parallel R_L)$$

$$v_o = (1+\beta) i_b (R_e \parallel R_L)$$

$$A_v = \frac{(1+\beta) (R_e \parallel R_L)}{r_{be} + (1+\beta) (R_e \parallel R_L)}$$

若 $(1+\beta) (R_e \parallel R_L) \gg r_{be}$, $A_v \approx 1$, $v_o \approx v_i$ 电压跟随器 / 射极跟随器



$$v_i = \frac{v_i}{R_b} + v_{be} = \frac{v_i}{R_b} + \frac{v_i}{r_{be} + (1+\beta)(R_e \parallel R_L)}$$

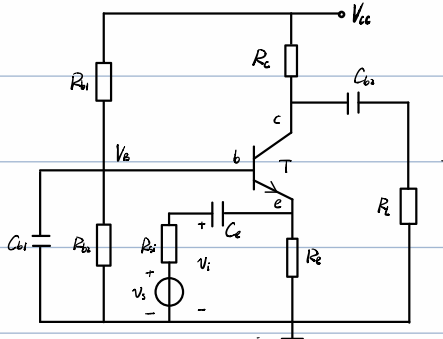
$$R_i = \frac{v_i}{i_i} = \frac{1}{\frac{1}{R_b} + \frac{1}{r_{be} + (1+\beta)(R_e \parallel R_L)}} = R_b \parallel [r_{be} + (1+\beta)(R_e \parallel R_L)]$$

$$v_t = i_b + \beta i_b + v_{Re} = \frac{(1+\beta)v_t}{R_{si} + r_{be}} + \frac{v_t}{R_e}$$

$$R_o = \frac{v_t}{i_t} = R_e \parallel \left(\frac{R_{si} + r_{be}}{1+\beta} \right)$$

- 特点**
- ① 电压增益小于1但接近1, v_o 与 v_i 同相
 - ② 输入电阻大, 对电压信号源衰减小
 - ③ 输出电阻小, 带电压负载能力强

(3) 共基极



$$v_o = -i_c (R_c \parallel R_L) = -\beta i_b (R_c \parallel R_L)$$

$$v_i = -i_b r_{be}$$

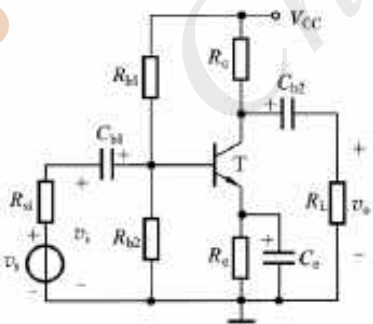
$$A_v = \frac{v_o}{v_i} = \frac{\beta (R_c \parallel R_L)}{r_{be}}$$

$$i_i = \frac{v_i}{R_e} - (1+\beta) i_b = \frac{v_i}{R_e} + \frac{(1+\beta)v_i}{r_{be}}$$

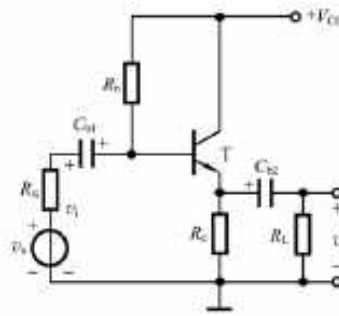
$$R_i = \frac{v_i}{i_i} = R_e \parallel \left(\frac{r_{be}}{1+\beta} \right)$$

$$R_o = R_c$$

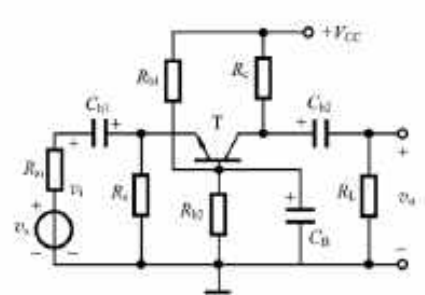
总结



共射极电路



共集电极电路



共基极电路

电压增益: $-\frac{\beta \cdot (R_c \parallel R_L)}{r_{be}}$

电压增益: $\frac{(1+\beta) \cdot (R_c \parallel R_L)}{r_{be} + (1+\beta)(R_c \parallel R_L)} \approx 1$

电压增益: $\frac{\beta \cdot (R_c \parallel R_L)}{r_{be}}$

输入电阻: $R_b \parallel r_{be}$

输入电阻: $R_b \parallel [r_{be} + (1+\beta)(R_c \parallel R_L)] \max$

输入电阻: $R_e \parallel \frac{r_{be}}{1+\beta} \min$

输出电阻: R_c

输出电阻: $R_e \parallel \frac{(R_{s1} \parallel R_b) + r_{be}}{1+\beta} \min$

输出电阻: R_c

相位关系: 反相

相位关系: 同相

相位关系: 同相

用途: 多级放大电路的中间级

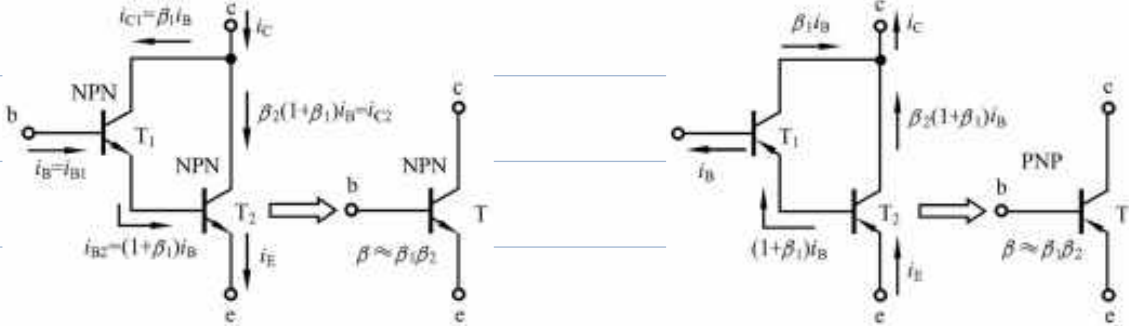
用途: 输入级、中间级、输出级

用途: 高频或宽频带电路

复合管

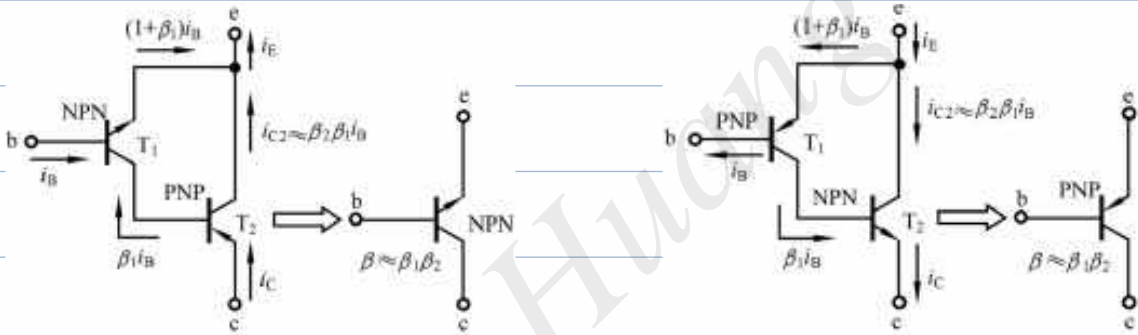
基本原则：BJT各电极电流方向不能冲突

同类型：T₁发射极 → T₂基极



等效基极-发射极电阻 $r_{be} = r_{be1} + (1 + \beta_1)r_{be2}$

不同类型：T₁集电极 → T₂基极

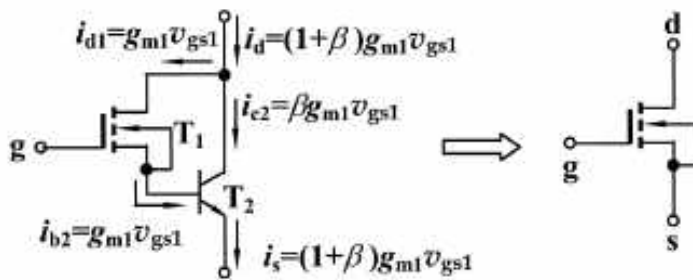


等效基极-发射极电阻 $r_{be} \approx r_{be1}$

复合管优点 ① 用简单的方法得到高β值三极管

② 分析电路时，可以简单地把它当作一个三极管

BiMOS复合管



$$\beta_m = (1 + \beta) g_{m1}$$

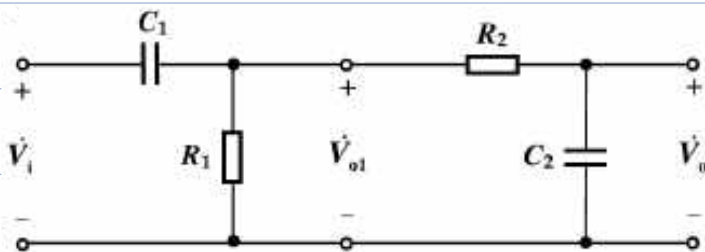
	增强型 NMOS 管	NPN 型 BJT
电路符号		
工作在放大区的两个条件	(1) 生成沟道 $v_{GS} \geq V_{TN}$ ($\approx 0.3 \sim 0.5V$, 现代工艺可达到的数值) (2) 沟道出现预夹断 $v_{DS} \geq v_{GS} - V_{TN}$	(1) 发射结正偏 $v_{BE} \geq V_{th}$ ($\approx 0.5V$) (2) 集电结反偏 或放宽为 $v_{BC} < 0.4V$ 且 $v_{CE} \geq 0.3V$
放大区的电流-电压关系	$i_D = \frac{\mu_n C_{ox}}{2} \cdot \frac{W}{L} (v_{GS} - V_{TN})^2 (1 + \lambda v_{DS})$ $= K_n (v_{GS} - V_{TN})^2 (1 + \lambda v_{DS})$ $i_G = 0$	$i_E \approx I_{ES} e^{v_{BE}/V_T}$ $i_C = \alpha i_E$ $i_B = i_C / \beta$
简化的低频小信号模型 (共源、共射)		
互导 (或跨导) g_m	$g_m = 2K_n (V_{GSQ} - V_{TN}) = 2\sqrt{K_n I_{DQ}}$	$g_m = \beta / r_{be} \approx I_{EQ} / V_T$
共源、共射连接时三极管的输入电阻	$r_{gs} = \infty$	$r_{be} = r_{bb'} + (1 + \beta) \frac{26mV}{I_{BQ} mA} \approx \frac{\beta}{g_m}$
三极管的输出电阻	$r_{ds} = [\lambda K_n (v_{GS} - V_{TN})^2]^{-1} = \frac{1}{\lambda I_{DQ}} = \frac{V_A}{I_{DQ}}$	$r_{ce} \approx \frac{V_A}{I_{CQ}}$

	反相电压放大电路	电压跟随器	电流跟随器
通用组态电路示意图			
组态命名依据的主要特征	不仅有 v_o 与 v_i 反相, 而且一般有 $ A_v \gg 1$	$v_o \approx v_i$, $A_v \approx 1$, 即 v_o 与 v_i 大小接近相等, 相位相同	$i_o \approx i_i$ 对于 BJT 有 $i_c \approx i_e$ 对于 FET 有 $i_d \approx i_s$
电路名称	共源极电路 共射极电路	共漏电极电路 共集极电路	共栅极电路 共基极电路
用途	电压增益高, 输入电阻和输入电容均较大, 适用于多级放大电路的中间级	输入电阻高、输出电阻低, 可作阻抗变换, 用于输入级、输出级或缓冲级	输入电阻小, 输入电容小, 适用于高频、宽带电路

§6 放大电路的频率响应

1 单时间常数 RC 电路的频率响应

1 个电阻 + 1 个电容



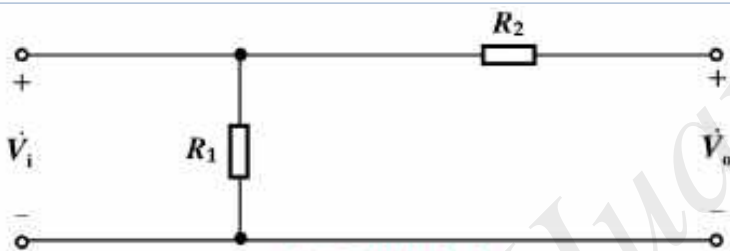
设 $R_1 C_1 \gg R_2 C_2$

且 $C_1 \gg C_2$ 时

(1) 中频响应 $\frac{1}{R_1 C_1} \ll \omega \ll \frac{1}{R_2 C_2}$

$\frac{1}{\omega C_1} \ll R_1$ C_1 可看作短路

$\frac{1}{\omega C_2} \gg R_2$ C_2 可看作开路

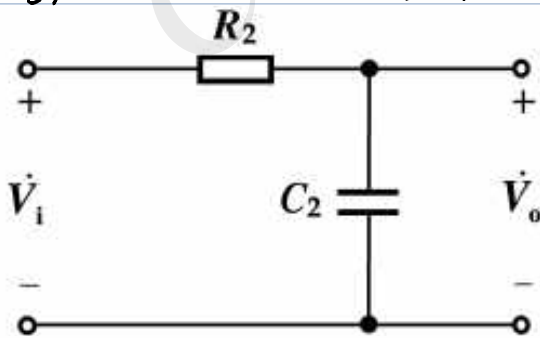


传递函数 (电压增益) $\dot{A}_{vm} = \frac{\dot{V}_o}{\dot{V}_i} = 1$

$|\dot{A}_{vm}| = 1$ $\varphi_m = \varphi_o - \varphi_i = 0$

(2) 高频响应 ω 接近或大于等于 $\frac{1}{R_2 C_2}$

$\frac{1}{\omega C_1} \ll R_1$ C_1 看作短路



RC 低通电路

$\dot{A}_{vh} = \frac{\dot{V}_o}{\dot{V}_i} = \frac{j\omega C_2}{R_2 + j\omega C_2} = \frac{1}{1 + j\omega R_2 C_2}$

令 $f_H = \frac{1}{2\pi R_2 C_2}$ 称为上限截止频率, $\omega = 2\pi f$

$\dot{A}_{vh} = \frac{1}{1 + j(\frac{f}{f_H})}$

电压增益的幅值 $|\dot{A}_{vh}| = \frac{1}{\sqrt{1 + (\frac{f}{f_H})^2}}$ 幅频响应

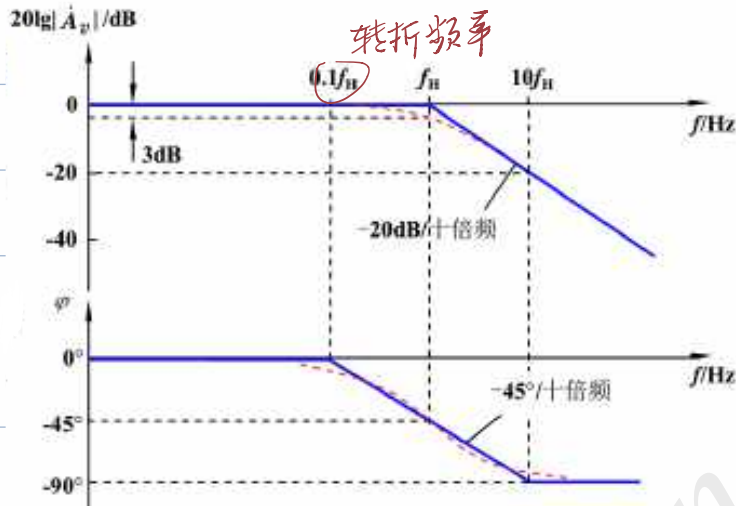
电压增益的相角 $\varphi_H = \varphi_o - \varphi_i = \arctan(\frac{f}{f_H})$ 相频响应

$$\text{幅频响应 } |A_{vH}| = \sqrt{1 + \left(\frac{f}{f_H}\right)^2}$$

当 $f \ll f_H$ 时, $|A_{vH}| \approx 1$, $20\lg|A_{vH}| = 0 \text{ (dB)}$

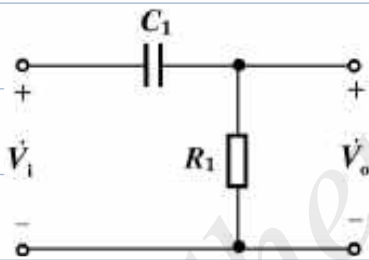
当 $f \gg f_H$ 时, $|A_{vH}| \approx \frac{f_H}{f}$, $20\lg|A_{vH}| \approx 20\lg f_H - 20\lg f \text{ (dB)}$

波特图:



(3) **低频响应** ω 接近或小于等于 $\frac{1}{R_1 C_1}$

$\frac{1}{\omega C_2} \gg R_2$ C_2 看作开路



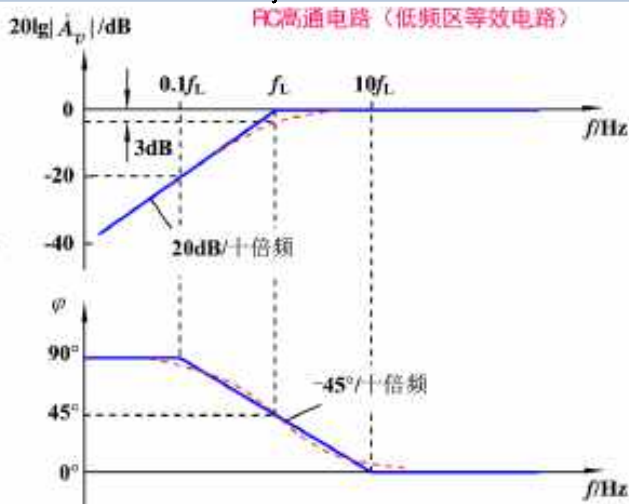
RC高通电路

$$A_{vL} = \frac{V_o}{V_i} = \frac{R_1}{R_1 + j\omega C_1} = \frac{1}{1 + j\omega R_1 C_1}$$

令 $f_L = \frac{1}{2\pi R_1 C_1}$ 称为下限截止频率, $\omega = 2\pi f$

$$A_{vL} = \frac{1}{1 + j\left(\frac{f}{f_L}\right)}$$

$$|A_{vL}| = \frac{1}{\sqrt{1 + \left(\frac{f}{f_L}\right)^2}} \quad \varphi_L = \varphi_o - \varphi_i = \arctan\left(\frac{f}{f_L}\right)$$

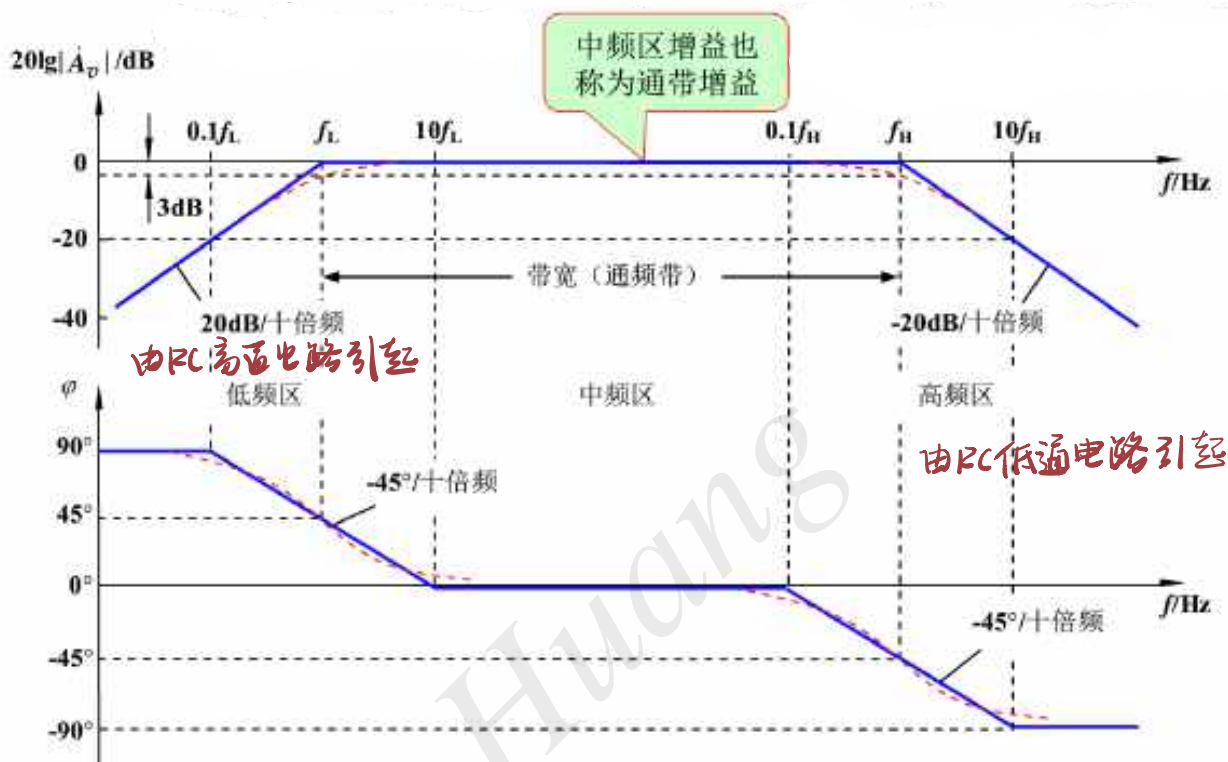


(4) 全频响应

上限频率: f_H

下限频率: f_L

带宽/通频带 $BW = f_H - f_L$ 当 $f_H \gg f_L$ 时, $BW \approx f_H$



结论

① f_H, f_L 取决于时间常数 $\tau = RC$

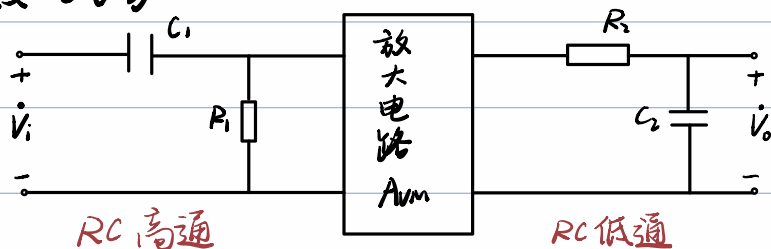
② 当输入信号的频率 $f = f_H$ 或 f_L 时, 电路增益比通带增益下降 3dB, 或下降为通带增益的 0.707 倍, 且在通带相移的基础上产生 -45° 或 45° 的相移。

③ 每个转折频率产生的衰减速率是每十倍频衰减 20dB

2 放大电路频率响应概述及三极管高频小信号模型

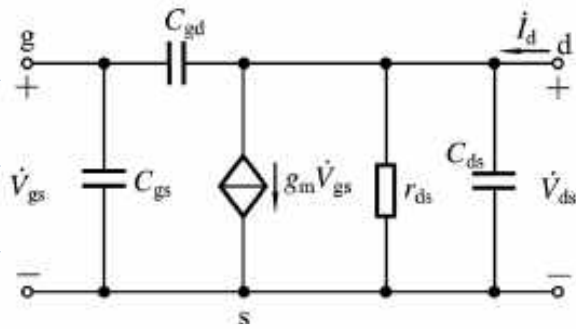
放大电路中存在: PN结电容、耦合电容、旁路电容 ...

等效电路:



$$R_1 C_1 \gg R_2 C_2$$

MOSFET 高频小信号模型



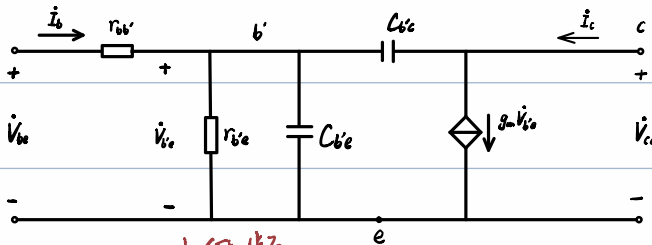
$$C_{gs} \approx 0.1 - 0.5 \text{ pF}$$

$$C_{gd} \approx 0.01 - 0.04 \text{ pF}$$

C_{ds} 更小

$$r_{ds} \approx 10^4 - 10^6 \Omega$$

BJT 高频小信号模型



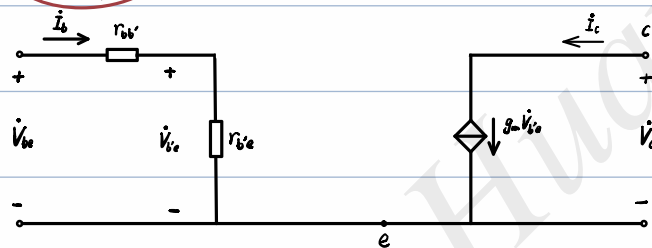
$$r_{bb'} \approx 200 \Omega$$

$$r_{be} = (1 + \beta) \frac{V_T}{I_{E0}}$$

C_{be} 约为几百 pF

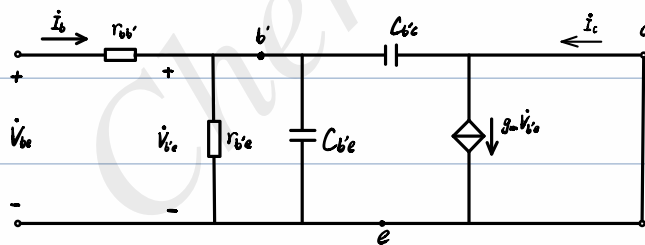
$$C_{bc} \approx 2 - 10 \text{ pF}$$

中低频
通带内 π 模型与小信号模型等价



$$g_m = \frac{\beta}{r_{be}} \approx \frac{I_{E0}}{V_T} \text{ 与频率无关}$$

β 的频率响应



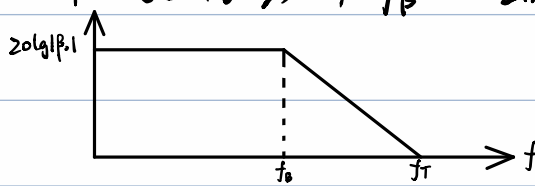
$$\begin{cases} I_c = g_m V_{be} - j\omega C_{bc} V_{bc} \\ I_b = \frac{V_{be}}{r_{be}} + j\omega C_{bc} V_{bc} + j\omega C_{be} V_{be} \end{cases}$$

$$\beta = \frac{I_c}{I_b} = \frac{g_m - j\omega C_{bc}}{\frac{1}{r_{be}} + j\omega(C_{bc} + C_{be})} \quad \text{又 } \beta_0 = g_m r_{be}$$

当 $g_m \gg \omega C_{bc}$ 时

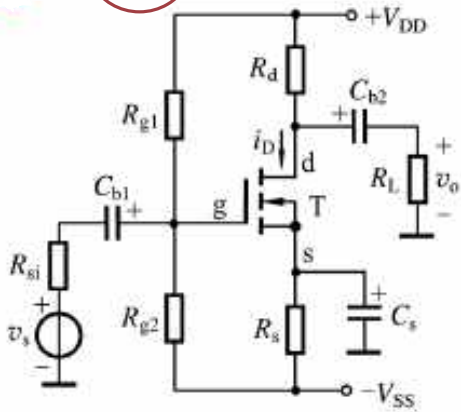
$$\beta = \frac{\beta_0}{1 + j\omega(C_{be} + C_{bc})r_{be}} \quad |\beta| = \frac{\beta_0}{\sqrt{1 + (f/f_0)^2}}$$

β 的上限频率 $f_\beta = \frac{1}{2\pi(C_{be} + C_{bc})r_{be}}$ 特征频率 f_T

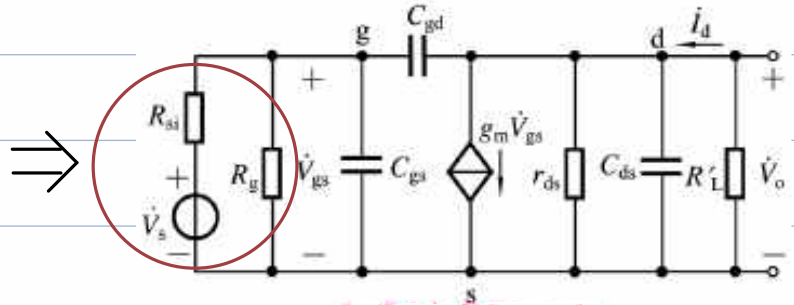


3 三极管放大电路的高频响应和带宽增益积

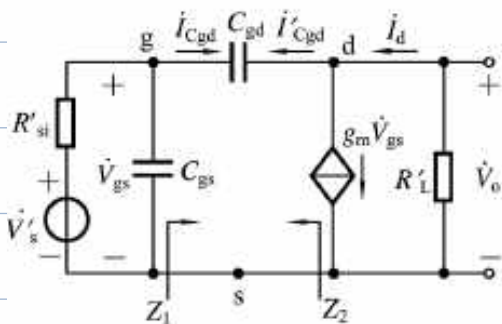
高频时耦合电容、旁路电容看作短路，直流电压源接地



$$R_g = R_{g1} \parallel R_{g2} \quad R_i' = R_d \parallel R_L$$



设 $r_{ds} \gg R_i'$, $V_s' = \frac{R_{si}}{R_{si} + R_g} V_s$ $R_{si} = R_{si} \parallel R_g$



设 $A_v' = \frac{v_o}{v_{gs}}$, 则

$$I_{Cgd} = \frac{v_{gs} - v_o}{j\omega C_{gd}} = (1 - A_v') v_{gs} \cdot j\omega C_{gd}$$

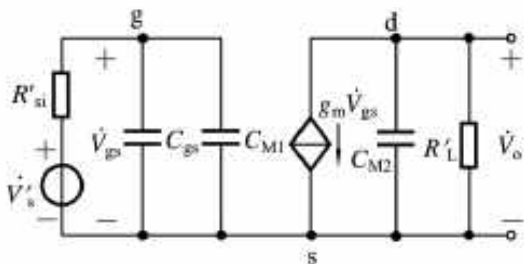
$$\text{阻抗 } Z_1 = \frac{v_{gs}}{I_{Cgd}} = (1 - A_v') \cdot j\omega C_{gd}$$

显然 Z_1 是一个电容的阻抗, $C_{m1} = (1 - A_v') C_{gd}$

同理 Z_2 也是一个电容的阻抗 $C_{m2} = (1 - \frac{1}{A_v'}) C_{gd}$

$i_d \approx g_m v_{gs}$, 则 $A_v' = \frac{v_o}{v_{gs}} = \frac{-i_d R_i'}{v_{gs}} = -g_m R_i'$

$$\begin{cases} C_{m1} = C_{gd} (1 + g_m R_i') \\ C_{m2} = C_{gd} (1 + \frac{1}{g_m R_i'}) \end{cases}$$



输入回路 $f \uparrow \Rightarrow |v_{gs}| \downarrow$

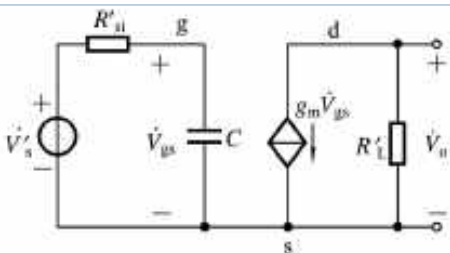
$R_{si} (C_{gs} + C_{m1})$ 为低通电路

输出回路 $f \uparrow \Rightarrow |v_o| \downarrow$

$R_i' C_{m2}$ 为低通电路

通常 $g_m R_i' \gg 1$, 则 $C_{m1} = C_{gd} (1 + g_m R_i') \gg C_{gd}$

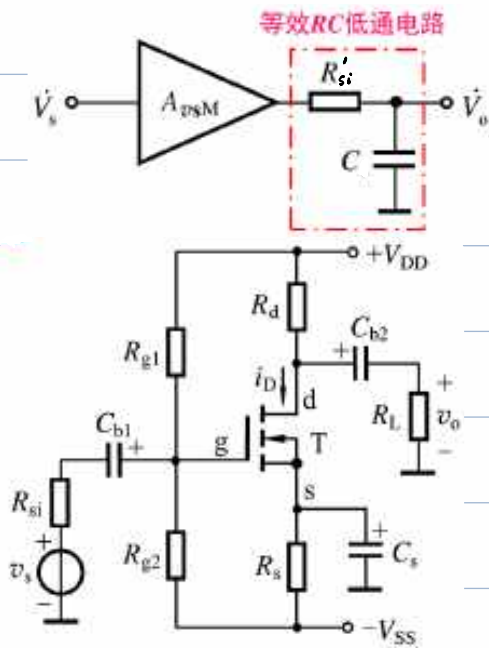
(开路) $C_{m2} = C_{gd} (1 + \frac{1}{g_m R_i'}) \approx C_{gd}$



通带内有 $v_{gs} = v_s'$

$$\begin{aligned} A_{vsm} &= \frac{v_o}{v_s} = \frac{v_o}{v_{gs}} \cdot \frac{v_{gs}}{v_s} = \frac{v_o}{v_{gs}} \cdot \frac{v_s'}{v_s} \\ &= -g_m R_i' \cdot \frac{R_{si}}{R_{si} + R_g} = -g_m R_i' \cdot \frac{R_g}{R_{si} + R_g} \end{aligned}$$

共源极放大电路的等效RC低通电路:



$$A_{vsm} = -g_m R_i' \frac{R_o}{R_{si} + R_o}$$

$$f_H = \frac{1}{2\pi R_{si} C}$$

哪些参数会影响上限频率?

$$R_{si} = R_{si} \parallel R_{g1} \parallel R_{g2} \quad \uparrow \text{明显提高}$$

$$C = C_{gs} + C_{mi} = C_{gs} + C_{gd}(1 + g_m R_i')$$

$$g_m = 2\sqrt{K_n I_{DQ}} \quad \text{选小的}$$

增益带宽积

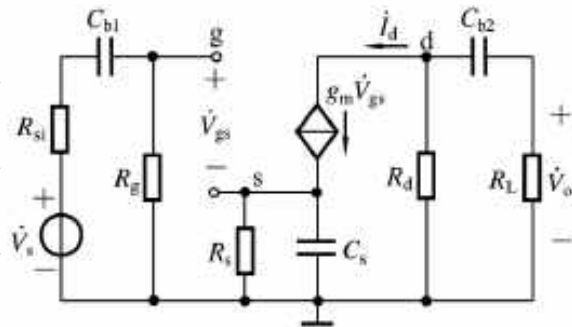
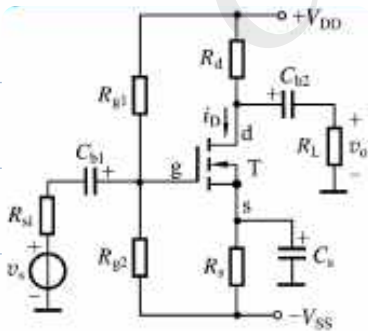
$$\begin{aligned} |A_{vsm} \cdot BW| &\approx |A_{vsm} \cdot f_H| = g_m R_i' \cdot \frac{R_o}{R_{si} + R_o} \cdot \frac{1}{2\pi R_{si} C} \\ &= g_m R_i' \cdot \frac{R_o}{R_{si} + R_o} \cdot \frac{1}{2\pi (R_{si} \parallel R_o) [C_{gs} + (1 + g_m R_i') C_{gd}]} \end{aligned}$$

通常有 $R_o \gg R_{si}$, $g_m R_i' \gg 1$, $(1 + g_m R_i') C_{gd} \gg C_{gs}$

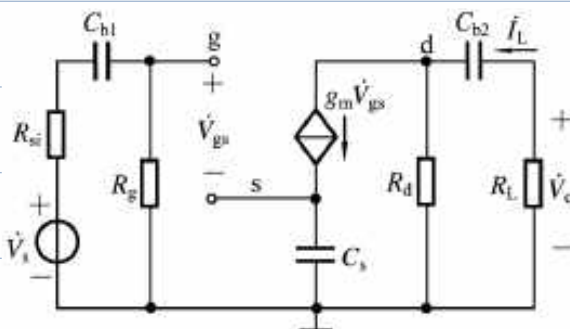
$$|A_{vsm} \cdot BW| \approx \frac{1}{2\pi R_{si} C_{gd}} \quad \text{近似为常数}$$

4 阻容耦合放大电路的低频响应及全频率响应

低频时 MOSFET 极间电容开路, 保留耦合电容和旁路电容.



设 C_s 足够大, $\frac{1}{\omega C_s} \ll R_s$



$$V_o = \frac{R_o}{R_{si} + R_o + \frac{1}{j\omega C_{b1}}} \cdot V_i$$

$$V_o = V_{gs} + g_m V_{gs} \frac{1}{j\omega C_s}$$

$$\Rightarrow V_{gs} = \frac{1}{1 + \frac{g_m}{j\omega C_s} \frac{R_o}{R_{si} + R_o + \frac{1}{j\omega C_{b1}}}} \cdot V_i$$

$$i_L = g_m V_{gs} \frac{R_d}{R_d + R_L + \frac{1}{j\omega C_{L2}}}$$

$$V_o = -i_L R_L = -g_m V_{gs} \frac{R_d}{R_d + R_L + \frac{1}{j\omega C_{L2}}} \cdot R_L$$

源电压增益

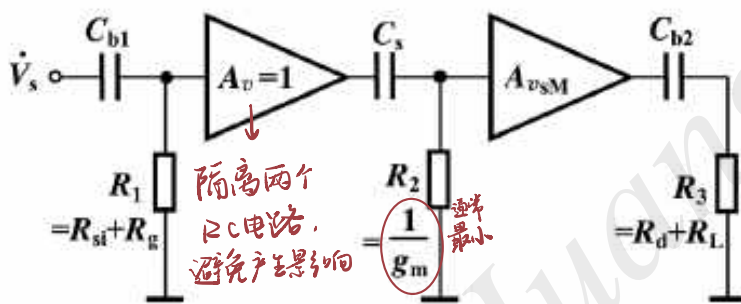
$$A_{v_{sL}} = \frac{V_o}{V_s} = \frac{V_o}{V_{gs}} \cdot \frac{V_{gs}}{V_s} = -g_m \frac{R_d}{R_d + R_L + \frac{1}{j\omega C_{L2}}} \cdot \frac{1}{1 + \frac{g_m}{j\omega C_s}} \cdot \frac{R_g}{R_{si} + R_g + \frac{1}{j\omega C_{b1}}}$$

$$= A_{v_{sM}} \cdot \frac{1}{1 - j(\frac{f_L}{f})} \cdot \frac{1}{1 - j(\frac{f_L}{f})} \cdot \frac{1}{1 - j(\frac{f_H}{f})}$$

其中 $A_{v_{sM}} = -g_m R_L' \frac{R_g}{R_{si} + R_g}$

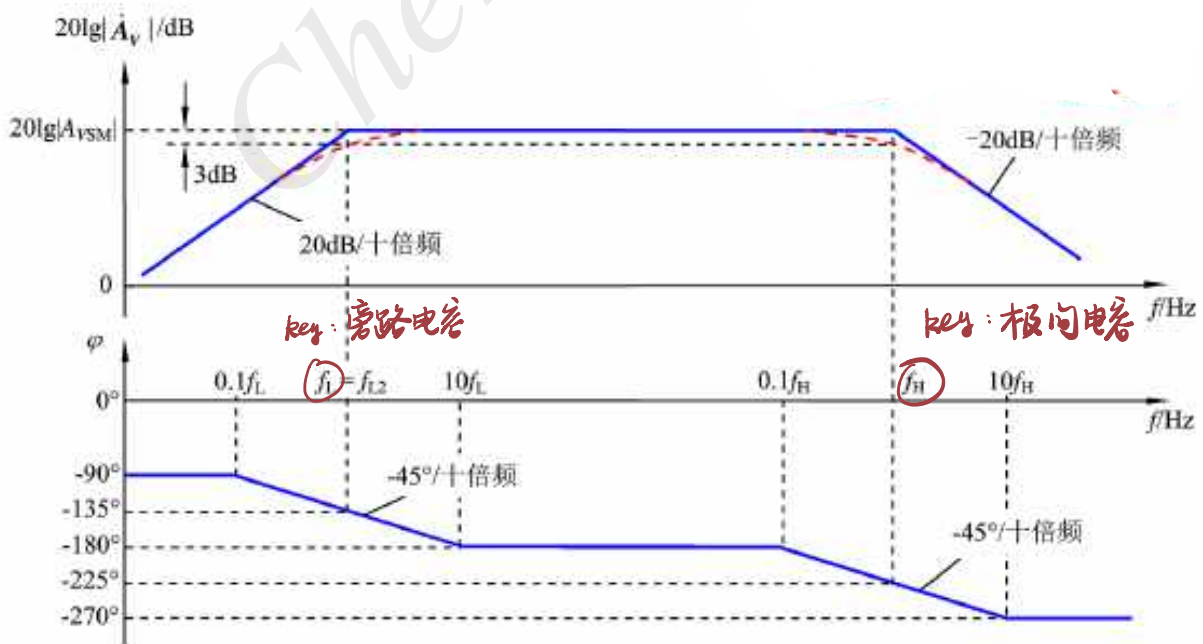
下限频率 $f_{L1} = \frac{1}{2\pi(R_{si} + R_g)C_{b1}}$ $f_{L2} = \frac{1}{2\pi(\frac{1}{g_m})C_s}$ $f_{L3} = \frac{1}{2\pi(R_d + R_L)C_{L2}}$

等效模型:



若 $f_{L2} > 4f_{L1}$, $f_{L3} > 4f_{L2}$, 则 $f_L \approx f_{L1}$

全频率响应



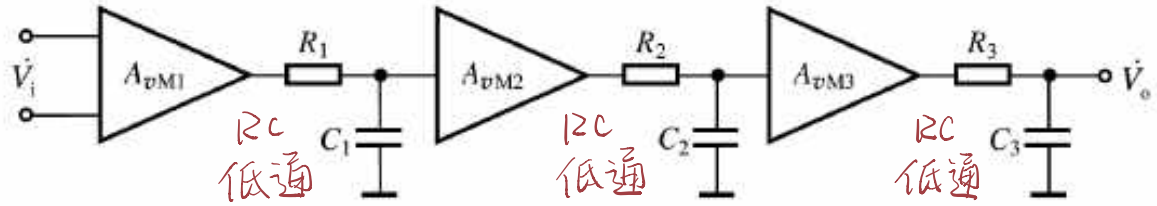
共源极放大电路的低频响应波特图 (忽略了 f_{L1} 和 f_{L3} 的影响)

增大带宽 \rightarrow 增大 f_H \rightarrow 选极间电容小的三极管

5 多级放大电路的频率响应

(1) 直接耦合多级放大电路

每级都可以等效成一个与频率无关的放大电路和一个RC低通电路的串联



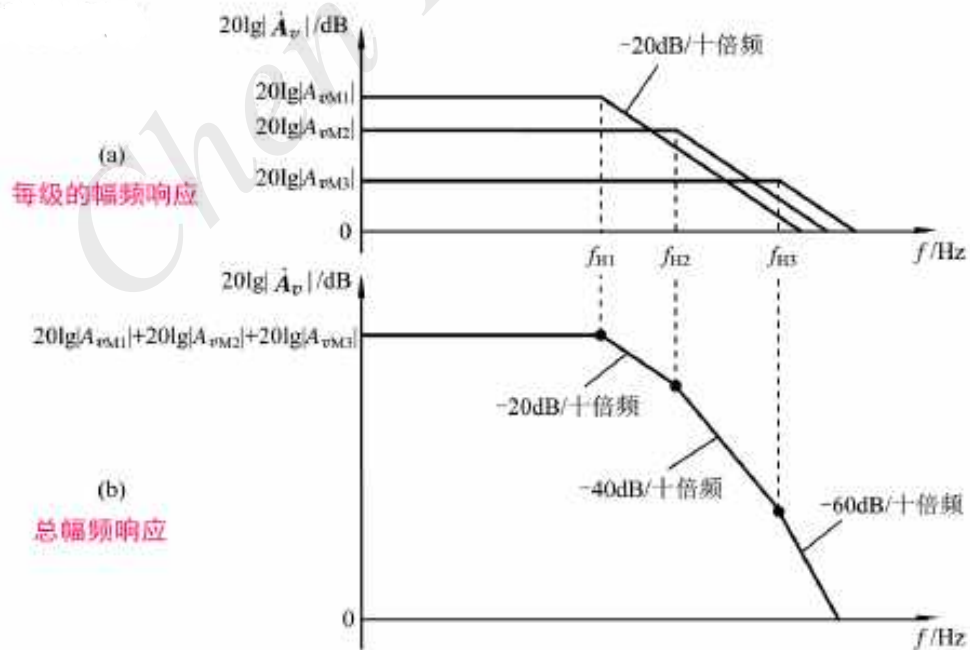
$$\begin{aligned} \dot{A}_{vH} &= \dot{A}_{vH1} \dot{A}_{vH2} \dot{A}_{vH3} \\ &= \frac{A_{vM1}}{1+j(\frac{f}{f_{H1}})} \cdot \frac{A_{vM2}}{1+j(\frac{f}{f_{H2}})} \cdot \frac{A_{vM3}}{1+j(\frac{f}{f_{H3}})} \end{aligned}$$

转折频率 $f_{H1} = \frac{1}{2\pi R_1 C_1}$ $f_{H2} = \frac{1}{2\pi R_2 C_2}$ $f_{H3} = \frac{1}{2\pi R_3 C_3}$

幅频响应 $|\dot{A}_{vH}| = |\dot{A}_{vH1}| \cdot |\dot{A}_{vH2}| \cdot |\dot{A}_{vH3}|$

$$= \frac{|A_{vM1}|}{\sqrt{1+(f/f_{H1})^2}} \cdot \frac{|A_{vM2}|}{\sqrt{1+(f/f_{H2})^2}} \cdot \frac{|A_{vM3}|}{\sqrt{1+(f/f_{H3})^2}}$$

$$20 \lg |\dot{A}_{vH}| = 20 \lg |\dot{A}_{vH1}| + 20 \lg |\dot{A}_{vH2}| + 20 \lg |\dot{A}_{vH3}|$$



相频响应 (设通带内无反相)

$$\varphi_H = -\arctan(\frac{f}{f_{H1}}) - \arctan(\frac{f}{f_{H2}}) - \arctan(\frac{f}{f_{H3}})$$

(2) 阻容耦合多级放大电路的频率响应

设 $A_{vm2} = A_{vm1}$, $f_{L2} = f_{L1}$, $f_{H2} = f_{H1}$

则总增益 $(0.707 A_{vm1})^2 = 0.5 A_{vm1}^2 < 0.707 A_{vm1}^2$

$\Rightarrow f_L > f_{L1}$, $f_H < f_{H1}$

多级放大电路的通频带一定比构成它的任何一级都窄

跨接在输入输出端口之间的电容会产生密勒效应

